

# Gradient-Based Quantification of Epistemic Uncertainty for Deep Object Detectors

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## Abstract

We study *gradient-based* epistemic uncertainty metrics [1] for deep object detectors to obtain reliable confidence estimates. We show that they contain predictive information and that they *capture information orthogonal* to that of common, output-based uncertainty estimation methods. Moreover, we use meta classifiers as a *post-processing filter mechanism* to the object detection pipeline and compare object detection performance. Our results show that gradient-based uncertainty is itself on par with output-based methods across different datasets and that combined meta classifiers based on gradient and output-based metrics outperform the standalone models. This suggests that variational inference may be supplemented by gradient-based uncertainty to obtain improved confidence measures, contributing to down-stream applications of deep object detectors by *improving their probabilistic reliability*.

## Gradient Uncertainty for Object Detection

Given an input image  $\mathbf{x} \in \mathcal{X}$  and model weights  $\mathbf{w}$ , we regard the box prediction of  $\hat{N}_{\mathbf{x}}$  instances

$$\hat{\mathbf{y}}(\mathbf{x}, \mathbf{w}) = (\hat{\mathbf{y}}^1, \dots, \hat{\mathbf{y}}^{N_{\mathbf{x}}}), \quad \hat{\mathbf{y}}^j = (\hat{\xi}^j, \hat{s}^j, \hat{\mathbf{p}}^j) \in \mathbb{R}^{4+1+C}, \quad (1)$$

consisting of a bounding box  $\hat{\xi}^j \in \mathbb{R}^4$ , an objectness score  $\hat{s}^j \in (0, 1)$  and a vector of class probabilities  $\hat{\mathbf{p}}^j \in (0, 1)^C$ . We compute the candidate-restricted self-learning gradient

$$g^{\text{cand}}(\mathbf{x}, \mathbf{w}, \hat{\mathbf{y}}^j) := \partial_{\mathbf{w}} \mathcal{L}(\text{cand}[\hat{\mathbf{y}}^j](\mathbf{x}, \mathbf{w}), \bar{\mathbf{y}}^j) \quad (2)$$

of  $\hat{\mathbf{y}}^j$  and generate scalars by measuring the magnitude of (2). The resulting uncertainty metrics are used as metrics  $\varphi$  for meta classification and meta regression.

**Theorem (Computational Complexity).** *The number of FLOP required to compute the last layer ( $t = T$ ) gradient is  $\mathcal{O}(k_T h w + k_T k_{T-1} (2s_T + 1)^4)$ . Similarly, for earlier layers  $t$ , we have  $\mathcal{O}(k_{t+1} k_t + k_t k_{t-1})$ , provided that we have previously computed the gradient for the consecutive layer  $t + 1$ . Performing variational inference only on the last layer requires  $\mathcal{O}(k_T k_{T-1} h w)$  FLOP per sample.*

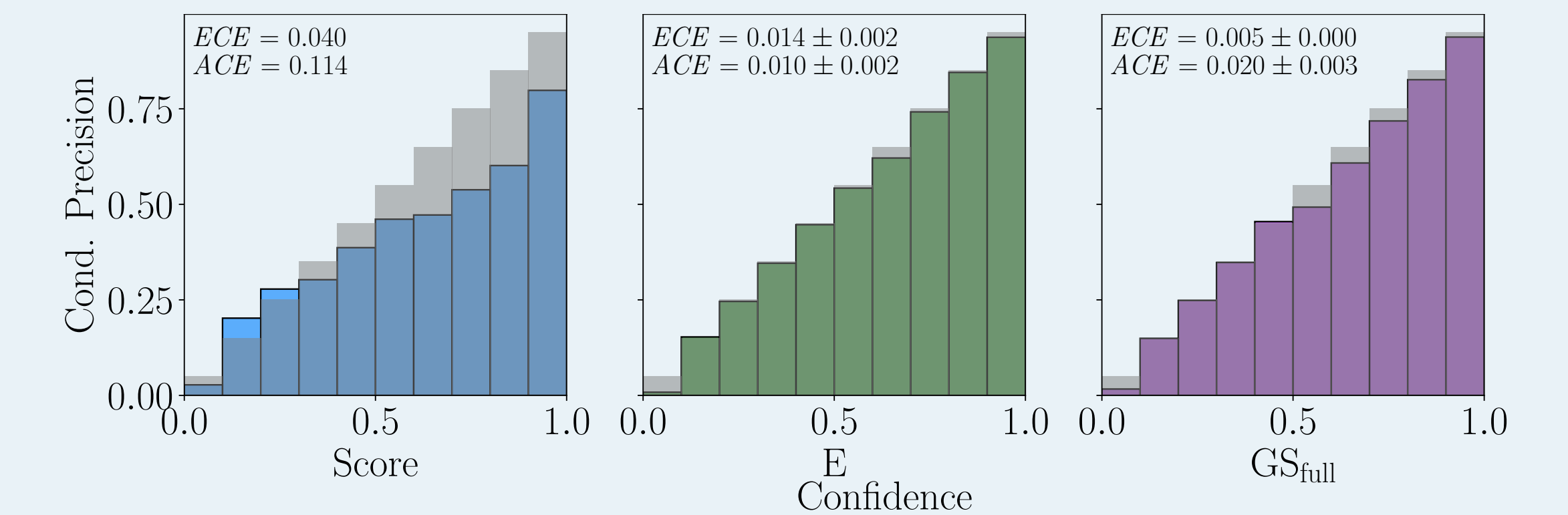
## References

[1] Tobias Riedlinger, Matthias Rottmann, Marius Schubert and Hanno Gottschalk *Gradient-Based Quantification of Epistemic Uncertainty for Deep Object Detectors*. preprint arXiv:2107.04517 (2021)

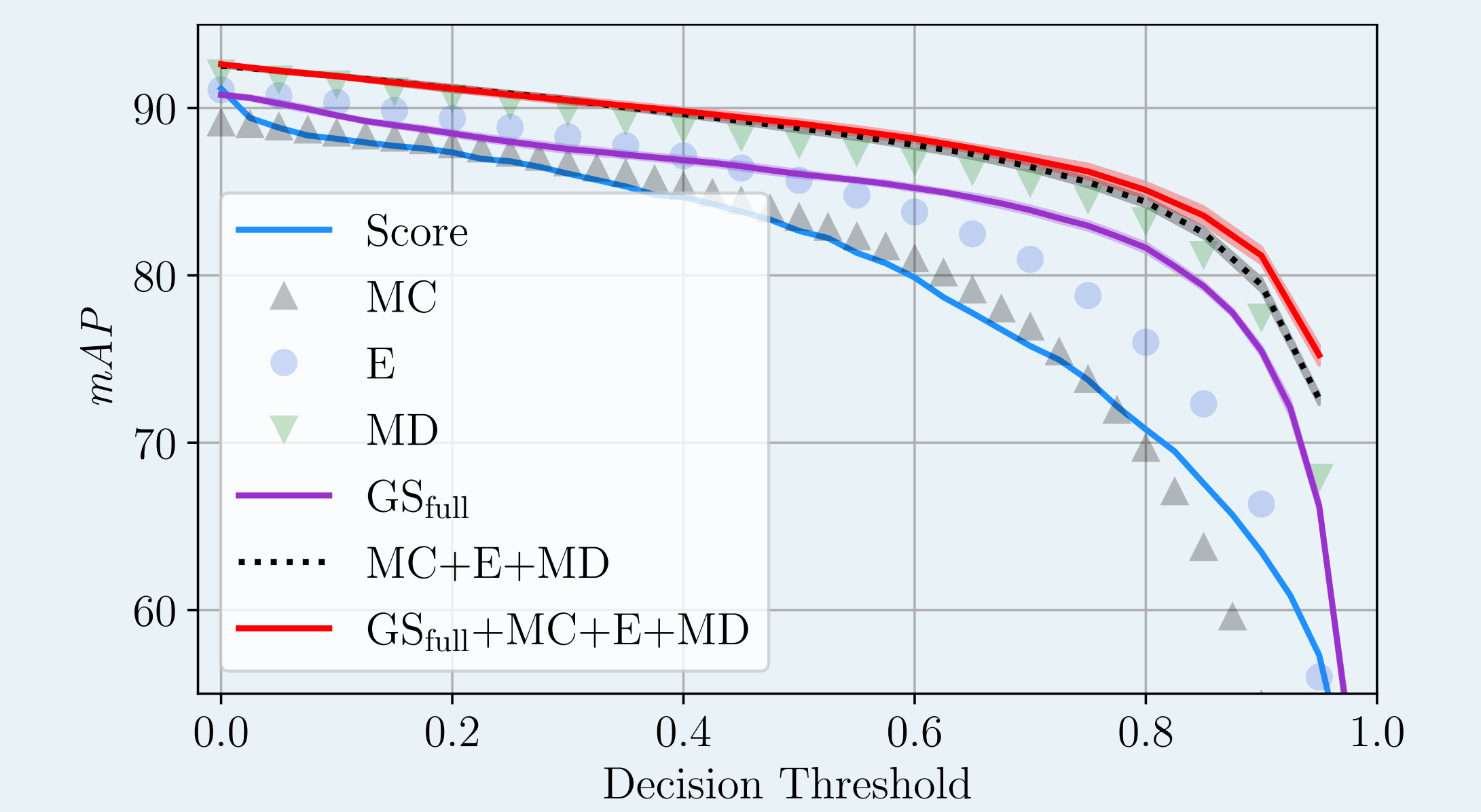
## Gradient-based Confidence Assignment



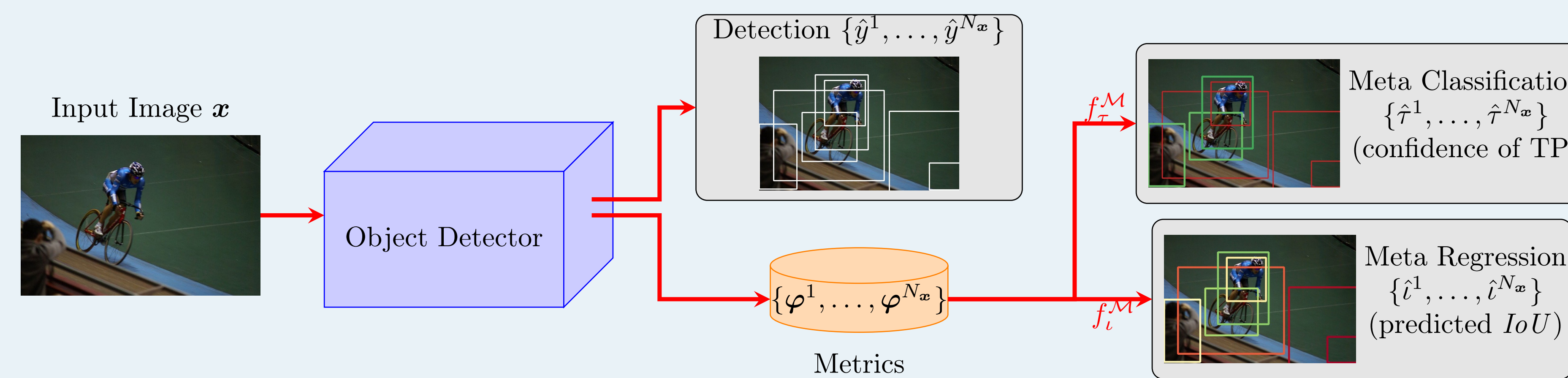
## Meta Classifier Calibration



## Object Detection Performance



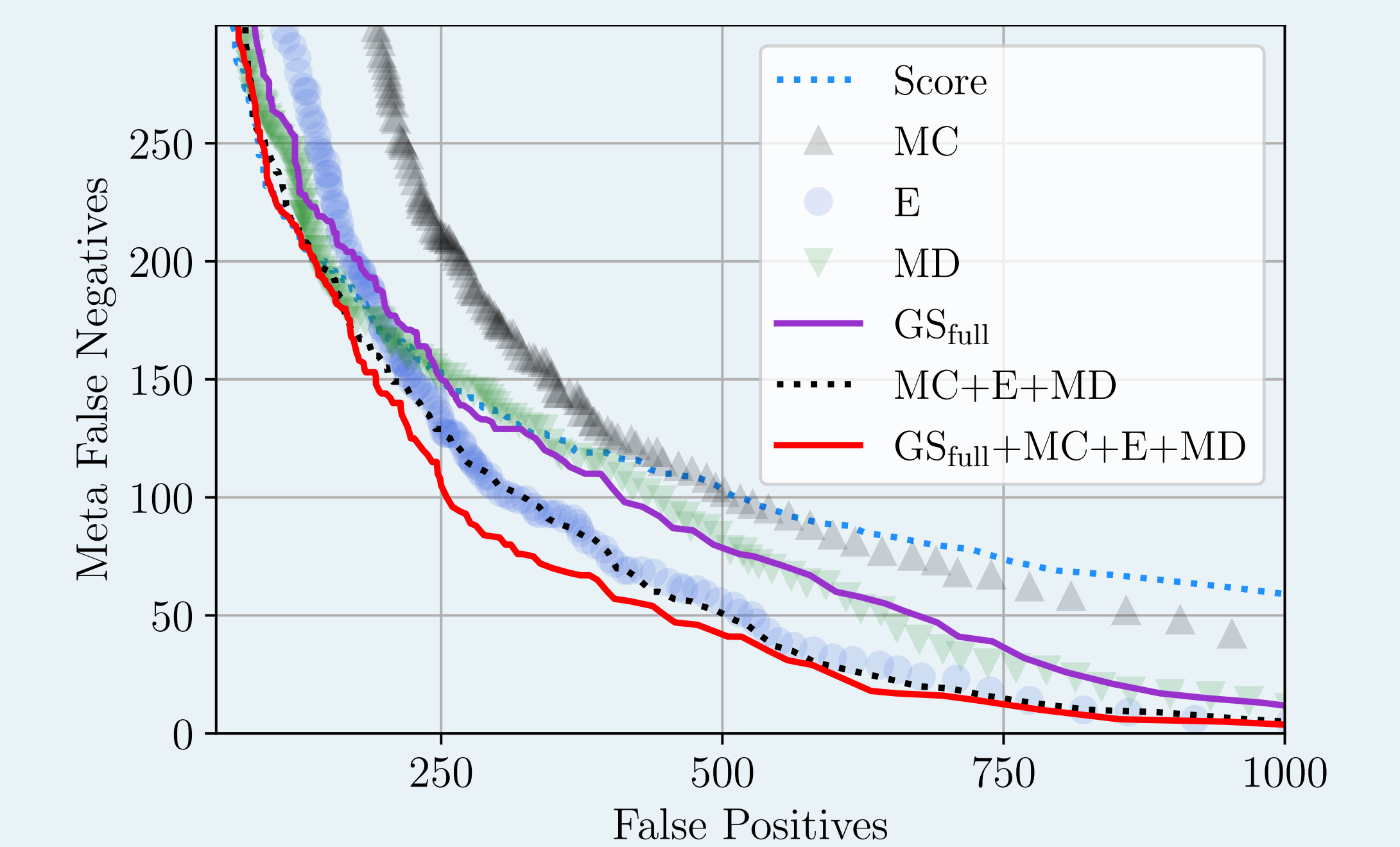
## Meta Classification and Meta Regression



YOLOv3	Pascal VOC		COCO		KITTI		YOLOv3	Pascal VOC	COCO	KITTI
Meta Classification	<i>AuROC</i>	<i>AP</i>	<i>AuROC</i>	<i>AP</i>	<i>AuROC</i>	<i>AP</i>	Meta Regression ( $R^2$ )			
Score	90.68 ± 0.06	69.56 ± 0.12	82.97 ± 0.04	62.31 ± 0.05	96.53 ± 0.05	96.87 ± 0.03	Score	48.29 ± 0.04	32.60 ± 0.02	78.86 ± 0.05
Entropy	91.30 ± 0.02	61.94 ± 0.06	76.52 ± 0.02	42.52 ± 0.04	94.79 ± 0.06	94.83 ± 0.05	Entropy	43.24 ± 0.03	21.10 ± 0.04	69.33 ± 0.04
Energy Score	92.59 ± 0.02	64.65 ± 0.06	75.39 ± 0.02	39.72 ± 0.06	95.66 ± 0.02	95.33 ± 0.03	Energy Score	47.18 ± 0.03	17.94 ± 0.02	71.53 ± 0.10
Full Softmax	93.81 ± 0.06	72.08 ± 0.15	82.91 ± 0.06	58.65 ± 0.10	97.07 ± 0.03	96.85 ± 0.03	Full Softmax	53.86 ± 0.11	36.95 ± 0.13	78.92 ± 0.11
MC Dropout (MC)	96.72 ± 0.02	78.15 ± 0.09	<b>89.04 ± 0.02</b>	64.94 ± 0.11	97.60 ± 0.07	97.17 ± 0.10	MC	61.63 ± 0.15	43.85 ± 0.09	82.10 ± 0.11
Ensemble (E)	<b>96.87 ± 0.02</b>	77.86 ± 0.11	88.97 ± 0.02	64.05 ± 0.12	97.63 ± 0.04	97.63 ± 0.05	E	61.48 ± 0.07	43.53 ± 0.13	84.18 ± 0.12
MetaDetect (MD)	95.78 ± 0.05	<b>78.64 ± 0.08</b>	87.16 ± 0.04	69.41 ± 0.07	<b>98.23 ± 0.02</b>	<b>98.06 ± 0.02</b>	MD	60.36 ± 0.14	<u>44.22 ± 0.11</u>	<b>85.88 ± 0.10</b>
Grad. Score $_{l_2}$ (GS $_{l_2}$ ; ours)	94.76 ± 0.03	74.86 ± 0.10	86.05 ± 0.04	64.25 ± 0.06	97.31 ± 0.05	96.86 ± 0.10	GS $_{l_2}$ (ours)	58.05 ± 0.13	38.77 ± 0.04	81.21 ± 0.05
Grad. Score $_{full}$ (GS $_{full}$ ; ours)	95.80 ± 0.04	<u>78.57 ± 0.11</u>	88.07 ± 0.03	<b>69.62 ± 0.07</b>	<u>98.04 ± 0.03</u>	97.81 ± 0.06	GS $_{full}$ (ours)	<b>62.50 ± 0.11</b>	<b>44.90 ± 0.09</b>	<u>85.40 ± 0.11</u>
MC+E+MD (ours)	97.66 ± 0.02	85.13 ± 0.12	91.14 ± 0.02	73.82 ± 0.05	98.56 ± 0.03	98.45 ± 0.03	MC+E+MD	69.38 ± 0.11	54.07 ± 0.08	87.78 ± 0.11
GS $_{full}$ +MC+E+MD (ours)	<b>97.95 ± 0.02</b>	<b>86.69 ± 0.09</b>	<b>91.65 ± 0.03</b>	<b>74.88 ± 0.07</b>	<b>98.74 ± 0.02</b>	<b>98.62 ± 0.01</b>	GS $_{full}$ +MC+E+MD	<b>72.26 ± 0.08</b>	<b>56.14 ± 0.11</b>	<b>88.80 ± 0.07</b>

## Decision Rule Tradeoff

Meta classifiers restricted to the "Pedestrian" class in KITTI:



Compared with the Score baseline, we find a *reduction of upwards of 100 FPs at 100 FNs* when basing the decisions exclusively on gradient uncertainty. The combined model achieves a reduction of 250 FPs.

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